## FACULTY OF PURE AND APPLIED MATHEMATICS SUBJECT CARD

Name in Polish: Równania różniczkowe cząstkowe z zastosowaniami w przemyśle Name in English: Partial differential equations with applications in industry
Main field of study (if applicable):Applied Mathematics
Specialization (if applicable): Mathematics for Industry and Commerce
Level and form of studies: 1st/ 2nd* level, full-time / part-time*
Kind of subject: obligatory-/ optional / university-wide*
Subject code MAP2040
Group of courses YES / NO*

|  | Lecture | Classes | Laboratory | Project | Seminar |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Number of hours of <br> organized classes in <br> University (ZZU) | 30 | 30 |  |  |  |
| Number of hours of <br> total student workload <br> (CNPS) | 90 | 90 |  |  |  |
| Form of crediting | Examination / <br> crediting with <br> grade* | Examination / <br> crediting with <br> grade* | Examination / <br> crediting with <br> grade* | Examination / <br> crediting with <br> grade* | Examination / <br> crediting with <br> grade* |
| For group of courses <br> mark (X) final course | X |  |  |  |  |
| Number of ECTS points | 3 | 3 |  |  |  |
| including number of | 1 | 2 |  |  |  |
| ECTS points for practical <br> (P) classes | including number of | 2 |  |  |  |
| ECTS points for direct <br> teacher-student contact <br> (BK) classes |  |  |  |  |  |

*delete as applicable

## PREREQUISITES RELATING TO KNOWLEDGE, SKILLS AND OTHER COMPETENCES

1. Student knows and can apply classical notions and methods of real and complex analysis.
2. Student knows and can apply elementary notions and methods of ordinary differential equations.

## SUBJECT OBJECTIVES

C1 Study of basic notions and acquisition of knowledge in the area of differential equations.
C2 Study of basic applications of partial differential equations in science, technology and industry.
C3 Acquisition of basic abilities in mathematical modelling by partial differential equations.

## SUBJECT EDUCATIONAL EFFECTS

relating to knowledge the student:
PEK_W01 knows the most important theorems from main areas of differential equations PEK_W02 knows basics of modelling by differential equations in technology and natural sciences, especially in physics, chemistry and biology.
relating to skills the student:
PEK_U01 can analyze basic problems of differential equations,
PEK_U02 can construct mathematical models with the usage of differential equations in concrete applications of mathematics.
relating to social competences the student:
PEK_K01 can, without assistance, search for necessary information in the literature, also in foreign languages
PEK_K02 understands necessity of systematic and individual work on the material of the course.

| PROGRAMME CONTENT |  |  |  |  |
| :--- | :--- | :---: | :---: | :---: |
| Form of classes - lecture | Number of hours |  |  |  |
| Lec1 | A reminder of information concerning first order partial differential <br> equations. Methods of characteristics, weak solutions and shock waves. | 4 |  |  |
| Lec2 | Second order partial differential equations and their classification. <br> Physical motivations. | 2 |  |  |
| Lec3 | Parabolic equations and their applications (heat, diffusion). Initial- <br> boundary problems, method of separation of variables, Fourier <br> transform, fundamental solution, maximum principle. | 8 |  |  |
| Lec4 | Hyperbolic equations and their applications (vibration of strings, <br> membranes and beams; acoustical, mechanical and electromagnetic <br> waves). D'Alembert's solution, initial-boundary problems, method of <br> separation of variables, Kirchhoff's solution, Huygens' principle. | 8 |  |  |
| Lec5 | Elliptic equations and their applications (stationary temperature <br> distribution, gravitational and electrostatic potential). Boundary value <br> problems, eigenfunctions, Poisson's equation, Green's function. | 6 |  |  |
| Lec6 | The calculus of variations and its applications. Euler-Lagrange <br> equation, Lagrangian mechanics, geodesic equation, minimal surface <br> equation. | 2 |  |  |
|  | Total hours | $\mathbf{3 0}$ |  |  |
| Form of classes - Class |  |  |  | $\mathbf{3 0}$ |
| Cl1 | Solving of problems for differential equations and their applications. | Number of hours |  |  |
|  | Total hours | TEACHING TOOLS USED |  |  |

EVALUATION OF SUBJECT EDUCATIONAL EFFECTS ACHIEVEMENT

| Evaluation (F - forming <br> (during semester), $\mathrm{P}-$ <br> concluding (at semester <br> end) | Educational effect <br> number | Way of evaluating educational effect achievement |
| :--- | :--- | :--- |
| F1 | PEK_W01 <br> PEK_W02 <br> PEK_K01 | exam |
| F2 | PEK_U01 <br> PEK_U02 <br> PEK_K01 | Oral presentations, tests, written reports. |
| P=0.5*F1+0.5*F2 |  |  |

## PRIMARY AND SECONDARY LITERATURE

PRIMARY LITERATURE:
[1] S.J.Farlow, Partial Differential Equations for Scientists and Engineers, Dover Publications, 1993.
[2] R.Haberman, Applied Partial Differential Equations with Fourier Series and Boundary Value Problems, Pearson, 2012.
[3] A. N. Tichonow, A. A. Samarski, Równania fizyki matematycznej, PWN 1963.

## SECONDARY LITERATURE:

[1] J. Ockendon, S. Howison, A. Lacey \& A. Movchan, Applied Partial Differential Equations, Oxford University Press, Oxford 1999.
[2] L. C. Evans, Równania różniczkowe cząstkowe, PWN 2002.
SUBJECT SUPERVISOR (NAME AND SURNAME, E-MAIL ADDRESS)
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dr inż. Lukasz Płociniczak (lukasz.plociniczak@pwr.edu.pl)

MATHEMATICS FOR INDUSTRY AND COMMERCE

| Subject educational effect | Correlation between subject <br> educational effect and educational <br> effects defined for main field of <br> study and specialization (if <br> applicable)** | Subject <br> objectives*** | Programme <br> content*** | Teaching tool <br> number*** |
| :---: | :--- | :--- | :--- | :--- |
| PEK_W01 (knowledge) | K2MIC_W03 | C1-C3 | Lec1-Lec15 | 1,3 |
| PEK_W02 | K2MIC_W07 | C1-C3 | Lec1-Lec15 | 1,3 |
| PEK_U01 (skills) | K2MIC_U15 | C1-C3 | Cl1 | $2,3,4$ |
| PEK_U02 | K2MIC_U16 | C1-C3 | Cl1 | $2,3,4$ |
| PEK_K01 (competences) | K2MIC_K06 | C1-C3 | Lec1-Lec15 <br> C11 | $1,2,3,4$ |
| PEK_K02 | K2MIC_K01 | C1-C3 | Lec1-Lec15 <br> C11 | 1, 2, 3, 4 |

[^0]
[^0]:    ** - enter symbols for main-field-of-study/specialization educational effects
    *** - from table above

