| FACULTY OF PURE AND APPLIED MATHEMATICS |
| :--- |
| SUBJECT CARD |
| Name in Polish: Matematyczne przetwarzanie obrazów |
| Name in English: Mathematical Image Processing |
| Main field of study (if applicable): APPLIED MATHEMATICS |
| Specialization (if applicable): MODELLING, SIMULATION, OPTIMIZATION |
| Level and form of studies: 1st/ 2nd* level, full-time / part-time* |
| Kind of subject: obligatory/ optional / university-wide* |
| Subject code MAT001582 |
| Group of courses YES / NQ* |


|  | Lecture | Classes | Laboratory | Project | Seminar |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Number of hours of <br> organized classes in <br> University (ZZU) | 30 |  | 30 |  |  |
| Number of hours of <br> total student workload <br> (CNPS) | 150 |  |  |  |  |
| Form of crediting | Examination / <br> crediting with <br> grade* | Examination / <br> crediting with <br> grade* | Examination / <br> crediting with <br> grade* | Examination / <br> crediting with <br> grade* | Examination / <br> crediting with <br> grade* |
| For group of courses <br> mark (X) final course | X |  |  |  |  |
| Number of ECTS points | 5 |  | 2 |  |  |
| including number of <br> ECTS points for practical <br> (P) classes | 2 | 1,5 |  | 1,5 |  |
| including number of <br> ECTS points for direct <br> teacher-student contact <br> (BK) classes |  |  |  |  |  |

PREREQUISITES RELATING TO KNOWLEDGE, SKILLS AND OTHER COMPETENCES

1. Knows basic concepts of theory of partial differential equations
2. Knows MATLAB package for mathematical computing

| SUBJECT OBJECTIVES |
| :--- |
| C1 Study of mathematical models in image processing. |
| C2 Study of numerical methods for solving problems in image processing. |
| C3 Application of acquired knowledge to construction and analysis of mathematical models in |
| image processing |

Selating to knowledge: $\quad$ SUBJECT EDUCATIONAL EFFECTS
PEK_W01 knows basic models for image restoration
PEK_W02 knows basic variational models for image segmentation
PEK_W03 knows numerical methods for solving problems in image processing
relating to skills:
PEK_U01 be able to demonstrate the difference between known models of image restoration
PEK_U02 be able to demonstrate the difference between known models of image segmentation
PEK_U03 be able to apply numerical methods to solve mathematical problems in image
processing
relating to social competences:
PEK_K01 can, without assistance, search for necessary information in the literature.
PEK_K02 understands the need for systematic work on course material

| PROGRAMME CONTENT |  | Form of classes - lecture |
| :--- | :--- | :--- |
| Number of <br> hours |  |  |
| Lec 1 | Overview of fundamental problems in image processing. Representation of <br> images. Models of image degradation. | 2 |
| Lec 2 | Linear diffusion filter. Gaussian smoothing in the frequency domain. | 2 |
| Lec 3 | Nonlinear diffusion filters. Isotropic and anisotropic diffusion models. | 4 |
| Lec 4 | Discretization of the nonlinear diffusion filter. | 2 |
| Lec 5 | Introduction to variational models for image restoration. | 2 |
| Lec 6 | Image denoising by total variation regularization. | 2 |
| Lec 7 | First order numerical schemes for total variation minimization. | 4 |
| Lec 8 | Image deblurring model. | 2 |
| Lec 9 | Total variation model for image inpainting. | 2 |
| Lec 10 | The Mumford-Shah model for image segmentation and its approximations. | 4 |
| Lec 11 | Active contours model for image segmentation. | 4 |
|  | Total hours | $\mathbf{3 0}$ |


| Form of classes - laboratory |  | Number of <br> hours |
| :--- | :--- | :--- |
| Lab 1 | Basic operation on images. Degradation of images. Gaussian smoothing. | 4 |
| Lab 2 | Solving selected problems illustrating theory given in the lectures using <br> mathematical MATLAB package for numerical computing | 26 |
|  | Total hours | $\mathbf{3 0}$ |

## TEACHING TOOLS USED

N1. Lecture - traditional method supported by multimedial presentation
N2. Computer laboratory - working on a computer using MATLAB package for numerical computations
N3. Consultations
N4. Student's self work - work on the project
EVALUATION OF SUBJECT EDUCATIONAL EFFECTS ACHIEVEMENT

| Evaluation (F - forming <br> (during semester), P - <br> concluding (at semester end) | Educational effect number | Way of evaluating educational <br> effect achievement |
| :--- | :--- | :--- |
| F1 | PEK_W01, PEK_W02, PEK_W03, <br> PEK_U01, PEK_U02, PEK_U03, <br> PEK_K01, PEK_K02, | activity in the laboratory |
| F2 | PEK_W01, PEK_W02, PEK_W03, <br> PEK_U01, PEK_U02, PEK_U03, <br> PEK_K01, PEK_K02, | oral presentation, report |
| P==0.2*F1+0.8*F2 |  |  |

## PRIMARY AND SECONDARY LITERATURE

## PRIMARY LITERATURE:

[1] G. Aubert and P. Kornprobst „Mathematical Problems in Image Processing: Partial Differential Equations and the Calculus of Variations", Springer-Verlag, 2007.
[2] T. Chan and J. Shen „Image Processing and Analysis: Variational, PDE, Wavelet, and Stochastic Methods", SIAM, 2006.

## SECONDARY LITERATURE:

[1] O. Scherzer (Editor) „Handbook of Mathematical Methods in Imaging", SpringerVerlag, 2010.

## SUBJECT SUPERVISOR (NAME AND SURNAME, E-MAIL ADDRESS)

Dr Monika Muszkieta (monika.muszkieta@pwr.edu.pl)

## MATRIX OF CORRELATION BETWEEN EDUCATIONAL EFFECTS FOR SUBJECT

## MATHEMATICAL IMAGE PROCESSING MAPXXXX AND EDUCATIONAL EFFECTS FOR MAIN FIELD OF STUDY MATHEMATICS AND SPECIALIZATION MATHEMATICS FOR INDUSTRY AND COMMERCE

| Subject educational effect | Correlation between subject educational effect and educational effects defined for main field of study and specialization (if applicable)** | Subject objectives*** | Programme content*** | Teaching tool number*** |
| :---: | :---: | :---: | :---: | :---: |
| PEK_W01 <br> (knowledge) | K2MST_W04, K2MST_mso_W01 | C1, C2, C3 | Lec 1, Lec 2, <br> Lec 3, Lec 5, <br> Lec 6, Lec 8, <br> Lec 9 <br> Lab 1, Lab 2 | 1, 2, 3, 4 |
| PEK_W02 | $\begin{gathered} \text { K2MST_W06, } \\ \text { K2MST_mso_W02 } \end{gathered}$ | C1, C2, C3 | Lec 10, Lec 11 <br> Lab 1, Lab 2 | 1, 2, 3, 4 |
| PEK_W03 | $\begin{gathered} \text { K2MST_W07 } \\ \text { K2MST_W13 } \\ \text { K2MST_mso_W03 } \end{gathered}$ | C1, C2, C3 | Lec 4, Lec 7 <br> Lab 1, Lab 2 | 1, 2, 3, 4 |
| $\begin{gathered} \text { PEK_U01 } \\ \text { (skills) } \end{gathered}$ | K2MST_U04 <br> K2MST_U05, <br> K2MST_U06, <br> K2MST_mso_U01 | C1, C2, C3 | Lec 1, Lec 2, Lec 3, Lec 5, Lec 6, Lec 8, Lec 9 Lab 1, Lab 2 | 1, 2, 3, 4 |
| PEK_U02 | K2MST_U09 <br> K2MST_U16 K2MST_mso_U01 | C1, C2, C3 | Lec 10, Lec 11 <br> Lab 1, Lab 2 | 1, 2, 3, 4 |
| PEK_U03 | K2MST_U17 K2MST_U24 K2MST_U25 K2MST_mso_U03 | C1, C2, C3 | Lec 4, Lec 7 <br> Lab 1, Lab 2 | 1, 2, 3, 4 |
| $\begin{gathered} \text { PEK_K01 } \\ \text { (competences) } \end{gathered}$ | K2MST_K05 K2MST_K06 K2MST_mso_K01 | C1, C2, C3 | Lec 1- Lec 11, Lab 1, Lab 2 | 1, 2, 3, 4 |
| PEK_K02 | K2MST_K03 K2MST_K04 K2MST_mso_K02 | C1, C2, C3 | Lec 1- Lec 11, Lab 1, Lab 2 | 1, 2, 3, 4 |

** - enter symbols for main-field-of-study/specialization educational effects
*** - from table above

