

## WROCLAW UNIVERSITY OF TECHNOLOGY – PHD STUDIES

<b>FACULTY OF PURE AND APPLIED MATHEMATICS</b>
<b>SUBJECT CARD</b>
Course name in Polish: Zastosowania Równań Różniczkowych Częstkowych
Course name in English: Applied Partial Differential Equations
Course language: Polish
University-wide general course type: 1) <u>basic course (mathematics, physics, chemistry, other)</u> 2) humanity course 3) managerial skills 4) English language 5) other modern language Departmental course developing professional skills: 1) specialized course 2) interdisciplinary course 3) seminar (interdisciplinary, specialized, departmental)
Type of course (obligatory, optional)
<b>Educational effects according to ZW 26/2017 regulations:  P8S_WG, P8S_UW, P8S_KK, P8S_KR</b>
Subject code: MAT1310

\*delete as applicable

	Lecture
Number of hours of organized classes in University (ZZU)	30
Number of hours of total student workload (CNPS)	90
Form of crediting	Exam
Number of ECTS points	3
including number of ECTS points for practical (P) classes	
including number of ECTS points for direct teacher-student contact (BK) classes	2

<b>PREREQUISITES RELATING TO KNOWLEDGE, SKILLS AND OTHER COMPETENCES</b>	
1.	Student knows the basic theory of calculus, ordinary differential equations and vector fields.
2.	Student is able to search for supplementary material in various areas of knowledge.

<b>SUBJECT OBJECTIVES</b>	
C1	Student will learn selected topics in the theory and applications of partial differential equations
C2	Student will acquire skills of applying learnt material in fields where there is a need for using partial differential equations.

## WROCLAW UNIVERSITY OF TECHNOLOGY – PHD STUDIES

<b>SUBJECT EDUCATIONAL EFFECTS</b>	
<b>Relating to knowledge:</b>	
PEK_W01 – Student knows the most important analytical methods for solving partial differential equations	
PEK_W02 – Student possesses knowledge concerning applications of differential equations in various fields of science.	
<b>Relating to skills:</b>	
PEK_U01 – Student gains skills needed to perform his/her research.	
PEK_U02 – Student is able to conduct his/her research.	
<b>Relating to social competences:</b>	
PEK_K01 – Student is aware of the role of cooperation, including an international cooperation.	
PEK_K02 – Student is aware of the importance of the original research activity	

<b>PROGRAM CONTENTS</b>		
<b>Form of classes – lecture</b>		Number of hours
Lec 1	The meaning of differential equations in mathematical modelling. Examples introducing partial differential equations of the first degree. Conservation laws.	2
Lec 2	Method of characteristics and Charpit's. Eikonal equation.	2
Lec 3	Inviscid Burgers equations: weak solutions. Rankine-Hugoniot's condition. Shock waves. Applications in various sciences.	4
Lec 4	Systems of first order equation. Shallow water equations and gas dynamics. A model of A-bomb (or supernova) explosion.	4
Lec5	Derivation of the heat equation. Separation of variables. Fundamental solution. Solution of Cauchy problem on several domains. Applications in technology, physics and geology.	4
Lec6	Free-boundary problems. Stefan problem. A model of freezing lake.	2
Lec7	Nonlinear parabolic equations. Self-similar solutions. Porous medium equation and Barenblatt's solution. A model of glacier movement. Fisher's equation.	2
Lec8	Gravitational potential and derivation of the Laplace and Poisson equations. Remark concerning separation of variables. Fundamental solution and Green's function. Integral representation of solutions. Applications in electrostatics, geological surveying and astrophysics.	4
Lec9	Derivation of vibrating string equations and its generalization for higher dimension. d'Alembert's and spherically symmetric solutions. Mechanical, acoustic and electromagnetic waves.	4
Lec10	Derivation of the Navier-Stokes equations. Remark concerning existence and uniqueness. Primitive equations of geophysical fluid dynamics. Geostrophic balance. Taylor-Proudman Theorem. Weather forecast.	2
Total hours		30

**WROCLAW UNIVERSITY OF TECHNOLOGY – PHD STUDIES**

<b>TEACHING TOOLS USED</b>	
N1	lecture
N2	consultation
N3	homework: solving problems and exercises

<b>EVALUATION OF ACHIEVED SUBJECT EDUCATIONAL EFFECTS</b>		
<b>Evaluation:</b> F – forming (partial) C – concluding	Educational effect number	Way of evaluating achievement of educational effects
F1	PEK_U01, PEK_U02, PEK_W01, PEK_W02	attendance of lectures
F2	PEK_W01, PEK_W02, PEK_U01, PEK_U02, PEK_K01, PEK_K02	solving problems and exercises
$C = 0.5 \cdot F1 + 0.5 \cdot F2$		

<b>PRIMARY AND SECONDARY LITERATURE</b>
<p><b><u>PRIMARY LITERATURE:</u></b></p> <p>[1] R. Haberman, Applied Partial Differential Equations with Fourier Series and Boundary Value Problems, Pearson, 2012.</p> <p>[2] A.N. Tichonow, A. A. Samarski, Równania fizyki matematycznej, PWN, 1963.</p> <p>[3] J.D. Logan, An Introduction to Nonlinear Partial Differential Equations, John Wiley &amp; Sons, 2008.</p> <p>[4] P. Markowich, Applied Partial Differential Equations: A Visual Approach, Springer Science &amp; Business Media, 2007.</p> <p><b><u>SECONDARY LITERATURE:</u></b></p> <p>[1] G.B. Whitham, Linear and Nonlinear Waves, John Wiley &amp; Sons, 2011.</p> <p>[2] J. R. Ockendon, Applied Partial Differential Equations, Oxford University Press, 2003.</p> <p>[3] L.C. Evans, Równania różniczkowe cząstkowe, PWN, 2008.</p> <p>[4] W.A. Strauss, Partial Differential Equations, New York: Wiley, 1992.</p>

<b>SUBJECT SUPERVISOR</b> (NAME AND SURNAME, E-MAIL ADDRESS)
dr inż. Łukasz Płociniczak, lukasz.plociniczak@pwr.edu.pl

## WROCLAW UNIVERSITY OF TECHNOLOGY – PHD STUDIES

**MATRIX OF CORRELATION BETWEEN EDUCATIONAL EFFECTS  
FOR SUBJECT  
GAME THEORY  
AND EDUCATIONAL EFFECTS FOR MAIN FIELD OF STUDY  
Doctoral studies at Faculty of Pure and Applied Mathematics**

Subject educational effect	Correlation between subject educational effect and educational effects defined for main field of study and specialization (if applicable)**	Subject objectives***	Programme content***	Teaching tool number***
(knowledge) PEK_W01	P8S_WG	C1,C2	Lec1-10	N1, N2, N3
PEK_W02	P8S_WG	C1,C2	Lec1-10	N1, N2, N3
(skills) PEK_U01	P8S_UW	C2	Lec1-10	N2, N3
PEK_U02	P8S_UW	C2,C3	Lec1-10	N2, N3
(competences) PEK_K01	P8S_KK	C3	Lec1-10	N2, N3
PEK_K02	P8S_KR	C3	Lec1-10	N2, N3

\*\* - enter symbols for main-field-of-study/specialization educational effects

\*\*\* - from table above