## FACULTY OF MECHANICAL ENGINEERING

|  | SUBJECT CARD |
| :--- | :--- |
| Name in English | MATHEMATICAL ANALYSIS II |
| Name in Polish | ANALIZA MATEMATYCZNA II |

Main field of study (if applicable )
Specialization (if applicable)
Level and form of studies
Kind of subject
Subject code
Group of courses

## MATHEMATICAL ANALYSIS II <br> analiza Matematyczna II

|  | Lecture | Classes | Laboratory | Project | Seminar |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of hours of organized <br> classes in University (ZZU) | 15 | 15 |  |  |  |
| Number of hours of total student <br> workload (CNPS) |  |  |  |  |  |
| Form of crediting | exam | crediting with grade |  |  |  |
| For a group of courses mark the final <br> course (X) |  |  |  |  |  |
| Number of ECTS points | 2 |  | 2 |  |  |
| including number of ECTS points <br> for practical (P) classes |  |  |  |  |  |
| including number of ECTS points <br> for direct teacher-student contact <br> (BK) classes |  |  |  |  |  |

## PREREQUISITES RELATING TO KNOWLEDGE, SKILLS AND OTHER COMPETENCES

Knowledge of differential calculus and integration for functions of one variable.

## SUBJECT OBJECTIVES

C1 Exposition of basic notions and laws of multivariable differential calculus and its applications.
C2 Exposition of basic notions and laws for double integrals and their applications in geometry.
C3 Exposition of basic notions and laws concerning improper integrals. Exposition of the basic criteria for convergence of numerical series and properties of power series.

## SUBJECT EDUCATIONAL EFFECTS

## Relating to knowledge a student:

PEK_W1 knows rudiments of multivariable differential calculus,
PEK_W2 has basic knowledge of double integrals and knows their applications,
PEK_W3 has basic knowledge of improper integrals of type I and numerical and function series.

## Relating to skills a student:

PEK_U1 can compute partial derivatives, the gradient and directional derivatives of multivariate functions and use them to find local extrema of multivariate functions,
PEK_U2 can calculate integrals of functions of two variables and apply integral calculus geometry and physics,
PEK_U3 can verify convergence of improper integrals of type I and numerical and function series and can construct power series approximating given functions of one variable.

## Relating to social competences a student:

PEK_K01_understands the need of systematic and independent work on mastery of the course material.

| PROGRAMME CONTENT |  | Fours of classes - lecture |
| :--- | :--- | :---: |
| Lec1 | Functions of several variables. The domain of a function of two variables. Graphs of <br> typical functions of two variables. The partial derivative. The plane tangent to the graph of <br> a function of two variables. The differential of multivariate function and its applications. | 2 |
| Lec2 | Directional derivatives. Gradient of a function. Higher order partial derivatives. | 2 |
| Lec3 | Local and global extrema. Sufficient conditions for the existence of the extreme. | 2 |
| Lec4 | The definite integral of a function of two variables. Geometric interpretation. Double <br> integrals over normal and regular regions. | 2 |
| Lec5 | Change of variables in double integrals. Double integrals in polar coordinates. <br> Applications of double integrals in geometry. | 2 |
| Lec6 | Improper integrals of type I. Comparison and limit comparison test. | 2 |
| Lec7 | Infinite numerical series. The basic criteria for convergence of series. Absolute <br> convergence. | 2 |
| Lec8 | Power series. Taylor and Maclaurin series. | 2 |
|  | Form of classes - classes | Hours |
| Cl1 | Partial derivatives. The plane tangent to the graph of a function of two variables. <br> Applications of the differential of multivariate function. | 2 |
| Cl2 | Directional derivatives. Gradient. Higher order partial derivatives. | 2 |
| Cl3 | Local and global extrema. | 1 |
| Cl4 | Calculation of double integrals over normal regions. | 2 |
| Cl5 | Double integrals in polar coordinates. Applications of double integrals in geometry. | 2 |
| Cl6 | Improper integrals of type I. | 1 |
| C17 | Infinite numerical series. | 2 |
| Cl8 | Power series. | 2 |
| Cl9 | Test. | 1 |
|  |  | $\mathbf{1 5}$ |

## TEACHING TOOLS USED

N1. Lecture - traditional method.
N2. Classes - traditional method (problems sessions and discussion).
N3. Student's self-study with the assistance of mathematical packages.
N4. Tutorial.

## EVALUATION OF SUBJECT EDUCATIONAL EFFECTS ACHIEVEMENT

| Evaluation (F-forming; <br> P - concluding) | Educational effect number | Way of evaluating educational effect achievement |
| :--- | :--- | :--- |
| F1 | PEK_U1-PEK_U3, <br> PEK_K1 | tests, oral presentations, quizzes |
| F2 | PEK_W1-PEK_W3 | exam |
| P - rules set by the lecturer |  |  |

## PRIMARY AND SECONDARY LITERATURE

## PRIMARY LITERATURE:

[1] W.G. McCallum et al., Multivariable calculus, John Wiley \& Sons, Inc.1997G.
[2] M. Gewert, Z. Skoczylas, Analiza matematyczna 2. Definicje, twierdzenia, wzory, Oficyna Wydawnicza GiS, Wrocław 2016.
[3] F. Leja, Rachunek różniczkowy i całkowy, PWN, Warszawa 2012.
[4] W.Żakowski, W.Kołodziej, Matematyka, cz. II, WNT, Warszawa 2014.

## SECONDARY LITERATURE:

[1] M. Gewert, Z. Skoczylas, Analiza matematyczna 2. Przykłady i zadania, Oficyna
a. Wydawnicza GiS, Wrocław 2016.
[2] W. Krysicki, L. Włodarski, Analiza matematyczna w zadaniach, Cz. II, PWN, Warszawa 2006.
[3] R. Leitner, Zarys matematyki wyższej dla studiów technicznych, Cz. 1-2, WNT, Warszawa 2006.

## SUBJECT SUPERVISORS

Wydziałowa Komisja Programowa ds. Kursów Ogólnouczelnianych
dr Marian Gewert (marian.gewert @ pwr.edu.pl)
doc. dr Zbigniew Skoczylas (zbigniew.skoczylas@ pwr.edu.pl)
CORRELATION MATRIX BETWEEN EDUCATIONAL EFFECTS FOR SUBJECT
MATHEMATICAL ANALYSIS II MAT001649
AND EDUCATIONAL EFFECTS FOR MAIN FIELD OF STUDY ......... AND SPECIALIZATION

| Subject <br> educational <br> effect | Correlation between subject <br> educational effect and educational <br> effects defined for main field of <br> study and specialization (if <br> applicable) | Subject <br> objectives | Programme content | Teaching tool <br> number |
| :---: | :---: | :---: | :---: | :---: |
| PEK_W1 |  | C1 | Lec1-Lec3 | N1-N4 |
| PEK_W2 |  | C2 | Lec4-Lec5 | N1-N4 |
| PEK_W3 |  | C3 | Lec6-Lec8 | N1-N4 |
| PEK_U1 |  | C1 | Cl1-Cl3 | N1-N4 |
| PEK_U2 | C2 | C14-Cl5 | N1-N4 |  |
| PEK_U3 |  | C3 | Cl6-C18 | N1-N4 |
| PEK_K1 |  | C1-C3 | Lec1-Lec8, Cl1-C19 | N1-N4 |

