

**FACULTY OF PURE AND APPLIED MATHEMATICS  
SUBJECT CARD**

**Name in Polish:** Zagadnienia ze swobodnym brzegiem

**Name in English:** Free boundary problems

**Main field of study (if applicable):** APPLIED MATHEMATICS

**Specialization (if applicable):** Mathematics for Industry and Commerce

**Level and form of studies:** 1st/ 2nd\* level, full-time / ~~part-time~~\*

**Kind of subject:** ~~obligatory~~/ optional / ~~university-wide~~\*

**Subject code** XXX

**Group of courses** YES / ~~NO~~\*

	Lecture	Classes	Laboratory	Project	Seminar
Number of hours of organized classes in University (ZZU)	30	30			
Number of hours of total student workload (CNPS)	150				
Form of crediting	Crediting with grade				
For group of courses mark (X) final course	X				
Number of ECTS points	5				
including number of ECTS points for practical (P) classes	2	2			
including number of ECTS points for direct teacher-student contact (BK) classes	1,5	1,5			

\*delete as applicable

**PREREQUISITES RELATING TO KNOWLEDGE, SKILLS AND OTHER COMPETENCES**

1. Student has basic knowledge and abilities in the area of ordinary and partial differential equations.

**SUBJECT OBJECTIVES**

C1 Study of mathematical models of phenomena in science and technology leading to free boundary problems.

C2 Study of basic analytical methods in examining free boundary problems.

**SUBJECT EDUCATIONAL EFFECTS**

relating to knowledge: student

PEK\_W01 knows basic mathematical models connected with free boundary problems.

PEK\_W02 knows basic analytical methods in examining free boundary problems.

relating to skills: student

PEK\_U01 can build mathematical models leading to free boundary problems.

PEK\_U02 can examine free boundary problems.

relating to social competences: student

PEK\_K01 is able to take benefits form scientific literature  
 PEK\_K02 knows limitations of his knowledge and understands the need of further education.

**PROGRAMME CONTENT**

<b>Form of classes - lecture</b>		<b>Number of hours</b>
Lec 1	Remaining basic theory of elliptic and parabolic partial differential equations.	2
Lec 2	Stefan problem, notion of the free boundary. Inverse Stefan problem.	2
Lec 3	Free boundary problems in melting and freezing. Modeling of problems connected with phase transition.	4
Lec 4	Modeling of flows in porous media: Boussinesq equation, porous media equation.	2
Lec 5	Self-similar solutions of porous media equation.	2
Lec 6	Free boundary in solutions of porous media equation, finite speed of propagation of disturbances. Retention and penetration property. Large time behavior of solutions.	2
Lec 7	Free boundary in reaction–diffusion–convection equations.	4
Lec 8	Diffusion in solids. Free boundary problems.	2
Lec 9	Modeling of flows in deformable media, spreading of impurities.	4
Lec 10	Free boundary problems in digital image processing.	2
Lec 11	Free boundary problems in financial mathematics.	2
Lec 12	Stationary free boundary problems: dam problem, obstacle problems in calculus of variations.	2
	Total hours	30
<b>Form of classes - class</b>		<b>Number of hours</b>
Cl 1	Solving of problems illustrating theory given on lectures.	30
	Total hours	<b>30</b>

**TEACHING TOOLS USED**

N1. Lecture – traditional method.  
 N2. Classes – traditional method.

**EVALUATION OF SUBJECT EDUCATIONAL EFFECTS ACHIEVEMENT**

<b>Evaluation</b> (F – forming (during semester), P – concluding (at semester end))	<b>Educational effect number</b>	<b>Way of evaluating educational effect achievement</b>

F1	PEK_W1, PEK_K1	Final test
F2	PEK_U1, PEK_U2, PEK_K1	Oral presentations, tests.
P= 0.5*F1+0.5*F2		
<b>PRIMARY AND SECONDARY LITERATURE</b>		
<b><u>PRIMARY LITERATURE:</u></b>		
[1]	R. M. Mattheij, S. W. Rienstra, J.H.M. ten Thije Boonkkamp, Partial Differential Equations, Modeling, Analysis, Computation, SIAM, Philadelphia 2005	
[2]	J. Ockendon, S. Howison, A. Lacey & A. Movchan, Applied Partial Differential Equations, Oxford University Press, Oxford 1999.	
[3]	A. Fasano, Parabolic Free Boundary Problems in Industrial and Biological Applications, SIMAI e-Lecture Notes, Volume 9, 2011	
<b><u>SECONDARY LITERATURE:</u></b>		
[1]	V. Alexiades, A.D. Solomon, Mathematical Modeling of Melting and Freezing Processes, Hemisphere – Taylor & Francis, Washington, DC, USA, 1983	
[2]	J.L. Vazquez, The Porous Media Equation, Mathematical Theory, Clarendon Press, Oxford 2007	
[3]	A.Friedman, Variational Principles and Free Boundary Problems, John Wiley and Sons, Inc	
<b>SUBJECT SUPERVISOR (NAME AND SURNAME, E-MAIL ADDRESS)</b>		
<b>Dr hab. Jan Goncerzewicz (<a href="mailto:Jan.Goncerzewicz@pwr.edu.pl">Jan.Goncerzewicz@pwr.edu.pl</a>)</b>		

MATRIX OF CORRELATION BETWEEN EDUCATIONAL EFFECTS FOR  
SUBJECT  
**FREE BOUNDARY PROBLEMS MAT001576**  
AND EDUCATIONAL EFFECTS FOR MAIN FIELD OF STUDY  
**APPLIED MATHEMATICS AND SPECIALIZATION**  
**MATHEMATICS FOR INDUSTRY AND COMMERCE**

Subject educational effect	Correlation between subject educational effect and educational effects defined for main field of study and specialization (if applicable)**	Subject objectives***	Programme content***	Teaching tool number***
<b>PEK_W01</b> (knowledge)	K2MST_W03 K2MST_mic_W01	C1, C2	Lec 1 - Lec 12	F1
<b>PEK_W02</b>	K2MST_W10 K2MST_mic_W02 K2MST_mic_W03	C1, C2	Lec 1 - Lec 12	F1
<b>PEK_U01</b> (skills)	K2MST_U15 K2MST_U24 K2MST_U25	C1, C2	C1 1	F2
<b>PEK_U02</b>	K2MST_U28 K2MST_U29 K2MST_U16	C1, C2	C1 1	F2
<b>PEK_K01</b> (competences)	K2MST_K06 K2MST_mic_K01	C1, C2,	Lec 1 - Lec 12, C1 1	F2
<b>PEK_K02</b>	K2MST_K01 K2MST_mic_K02	C1-C2	Wy1-Wy11, Ćw1	1, 2, 3, 4

\*\* - enter symbols for main-field-of-study/specialization educational effects

\*\*\* - from table above