

**FACULTY OF PURE AND APPLIED MATHEMATICS  
SUBJECT CARD**

**Name in Polish:** Wstęp do matematycznych metod przetwarzania obrazu

**Name in English:** Introduction to Mathematical Image Processing

**Main field of study (if applicable):** Applied Mathematics

**Specialization (if applicable):** Mathematics for Industry and Commerce

**Level and form of studies:** 1st/ 2nd\* level, full-time / ~~part-time~~\*

**Kind of subject:** ~~obligatory~~-/ optional / ~~university-wide~~\*

**Subject code** MAT1549

**Group of courses** YES / ~~NO~~\*

	Lecture	Classes	Laboratory	Project	Seminar
Number of hours of organized classes in University (ZZU)	30		30		
Number of hours of total student workload (CNPS)	90		60		
Form of crediting	<del>Examination</del> / crediting with grade*	Examination / crediting with grade*	Examination / crediting with grade*	Examination / crediting with grade*	Examination / crediting with grade*
For group of courses mark (X) final course	X				
Number of ECTS points	3		2		
including number of ECTS points for practical (P) classes			2		
including number of ECTS points for direct teacher-student contact (BK) classes	1,5		1,5		

\*delete as applicable

**PREREQUISITES RELATING TO KNOWLEDGE, SKILLS AND OTHER COMPETENCES**

1. Student knows basic concepts of functional analysis
2. Knows basic concepts of theory of partial differential equations
3. Knows and can apply basic methods of variational calculus
4. Knows at least one package for mathematical computing
5. Knows basic numerical methods for solving partial differential equations

**SUBJECT OBJECTIVES**

C1 Study of fundamental mathematical models in image processing

C2 Study of numerical methods for solving problems of filtering, segmentation and decomposition of image

C3 Application of acquired knowledge to construction and analysis of mathematical models in image processing

### SUBJECT EDUCATIONAL EFFECTS

relating to knowledge:

PEK\_W01 knows basic models of image filtering

PEK\_W02 knows basic models of image segmentation

PEK\_W03 knows the Meyer decomposition model

PEK\_W04 knows numerical methods for solving fundamental problems in image processing

relating to skills:

PEK\_U01 be able to demonstrate the equivalence of known models of image filtering

PEK\_U02 be able to demonstrate the equivalence of known models of image segmentation

PEK\_U03 be able to apply numerical methods to solve approximate solutions to mathematical models in image processing

relating to social competences:

PEK\_K01 can, without assistance, search for necessary information in the literature.

PEK\_K02 understands the need for systematic work on course material

### PROGRAMME CONTENT

<b>Form of classes - lecture</b>		<b>Number of hours</b>
Lec 1	Overview of fundamental problems in image processing. Image degradation models	2
Lec 2	Models of image denoising: linear diffusion filter, nonlinear diffusion filters, variational models for image denoising, wavelets models for image denoising, nonlocal filters.	12
Lec 3	Discretization of selected image denoising model	2
Lec 4	Models of image segmentation: variational model of Mumford-Shah and its approximations, stochastic model of Geman-Geman, active contours model	8
Lec 5	Discretization of selected image segmentation model	2
Lec 6	Image decomposition model of Meyer and methods of its solution	4
	<b>Total hours</b>	<b>30</b>
<b>Form of classes - laboratory</b>		<b>Number of hours</b>
Lab 1	Basic operation on images. Degradation of images	2
Lab 2	Implementation of nonlinear diffusion filter	6
Lab 3	Implementation of the algorithm for minimization of the Rudin, Osher and Fatemi model	4
Lab 4	Implementation of the algorithm for minimization of the Mumford-Shah model	6
Lab 5	Implementation of evolution equation related with the active contour model	6
Lab 6	Implementation of the algorithm for image decomposition	6
	<b>Total hours</b>	<b>30</b>

### TEACHING TOOLS USED

- N1. Lecture – traditional method supported by multimedial presentation  
 N2. Computer laboratory – working on a computer using a software package for numerical computations  
 N3. Consultations  
 N4. Student’s self work – preparation for the laboratory

### EVALUATION OF SUBJECT EDUCATIONAL EFFECTS ACHIEVEMENT

Evaluation (F – forming (during semester), P – concluding (at semester end))	Educational effect number	Way of evaluating educational effect achievement
F1	PEK_W04, PEK_U03,  PEK_K01,	activity in the laboratory, oral presentation, projects, raports
F2	PEK_W01,  PEK_W02,  PEK_W03,  PEK_W04,  PEK_U01,  PEK_U02,  PEK_U03,  PEK_K01,  PEK_K02,	test
$P=0.5 \cdot F1 + 0.5 \cdot F2$		

### PRIMARY AND SECONDARY LITERATURE

#### **PRIMARY LITERATURE:**

- [1] G. Aubert and P. Kornprobst „Mathematical Problems in Image Processing: Partial Differential Equations and the Calculus of Variations”, Springer-Verlag, 2007.  
 [2] T. Chan and J. Shen „Image Processing And Analysis: Variational, PDE, Wavelet, And Stochastic Methods”, SIAM, 2006.

#### **SECONDARY LITERATURE:**

- [1] O. Scherzer (Editor) „Handbook of Mathematical Methods in Imaging”, Springer-Verlag, 2010.

#### **SUBJECT SUPERVISOR (NAME AND SURNAME, E-MAIL ADDRESS)**

Dr Monika Muszkieta (Monika.Muszkieta@pwr.wroc.pl)

MATRIX OF CORRELATION BETWEEN EDUCATIONAL EFFECTS FOR  
SUBJECT

**Introduction to Mathematical Image Processing MAT1549**  
AND EDUCATIONAL EFFECTS FOR MAIN FIELD OF STUDY  
**APPLIED MATHEMATICS**  
AND SPECIALIZATION MATHEMATICS FOR INDUSTRY AND  
**COMMERCE**

Subject educational effect	Correlation between subject educational effect and educational effects defined for main field of study and specialization (if applicable)**Iności (o ile dotyczy)	Subject objectives***	Programme content***	Teaching tool number***
<b>PEK_W01</b> (knowledge)	K2MIC_W04, K2MIC_W06, K2MIC_W07, K2MIC_W13	C1, C3	Lec 1, Lec 2, Lab 2, Lab 3	1, 2, 3
<b>PEK_W02</b>	K2MIC_W04, K2MIC_W06, K2MIC_W07, K2MIC_W13	C1, C3	Lec 1, Lec 4, Lab 4, Lab 5	1, 2, 3
<b>PEK_W03</b>	K2MIC_W04, K2MIC_W06, K2MIC_W07, K2MIC_W13	C1, C3	Lec 6, Lab 6	1, 2, 3
<b>PEK_W04</b>	K2MIC_W08, K2MIC_W10, K2MIC_W12, K2MIC_W13	C2	Lec 3, Lec 5, Lab 1-Lab 6	1, 2, 3, 4
<b>PEK_U01</b> (skills)	K2MIC_U04, K2MIC_U05, K2MIC_U06, K2MIC_U09	C1, C3	Lec 2, Lab 2, Lab 3	1, 2, 3
<b>PEK_U02</b>	K2MIC_U04, K2MIC_U05, K2MIC_U06, K2MIC_U09	C1, C3	Lec 4, Lab 4, Lab 5	1, 2, 3
<b>PEK_U03</b>	K2MIC_U16, K2MIC_U17	C2	Lec 3, Lec 5, Lab 1-Lab 6	1, 2, 3, 4
<b>PEK_K01</b> (competences)	K2MIC_K05, K2MIC_K06	C1, C2, C3	Lec 1- Lec 6, Lab 1-Lab 5	1, 2, 3, 4
<b>PEK_K02</b>	K2MIC_K03, K2MIC_K04	C1, C2, C3	Lec 1- Lec 6, Lab 1-Lab 5	1, 2, 3, 4

\*\* - enter symbols for main-field-of-study/specialization educational effects

\*\*\* - from table above