

**FACULTY OF PURE AND APPLIED MATHEMATICS
SUBJECT CARD**

Name in Polish: METODY NUMERYCZNE W RÓWNANIACH RÓŻNICZKOWYCH

Name in English: Numerical methods in differential equations

Main field of study (if applicable): APPLIED MATHEMATICS

Specialization (if applicable): Mathematics for Industry and Commerce

Level and form of studies: ~~1st~~ 2nd* level, full-time / ~~part-time~~*

Kind of subject: ~~obligatory~~ / optional / ~~university-wide~~*

Subject code MAT001570

Group of courses YES / ~~NO~~*

	Lecture	Classes	Laboratory	Project	Seminar
Number of hours of organized classes in University (ZZU)	30		30		
Number of hours of total student workload (CNPS)	150				
Form of crediting	Examination / crediting with grade*	Examination / crediting with grade*	Examination / crediting with grade*	Examination / crediting with grade*	Examination / crediting with grade*
For group of courses mark (X) final course	X				
Number of ECTS points	5				
including number of ECTS points for practical (P) classes	2		2		
including number of ECTS points for direct teacher-student contact (BK) classes	1,5		1,5		

*delete as applicable

PREREQUISITES RELATING TO KNOWLEDGE, SKILLS AND OTHER COMPETENCES

1. Student has basic knowledge and abilities on mathematical analysis.
2. Student has basic knowledge concerning programming environments: Matlab/Mathematica/Mapple.

SUBJECT OBJECTIVES

- C1 Study of basic notions and knowledge in the area of numerical methods applied in differential equations
- C2 Study of basic numerical techniques used in discretization of differential equations.
- C3 Acquisition of basic abilities in constructing and analyzing difference schemes for differential equations

SUBJECT EDUCATIONAL EFFECTS

relating to knowledge student:

PEK_W01 knows the most important numerical techniques used in solving problems for differential equations

PEK_W02 knows bases of constructing own numerical schemes

relating to skills student:

PEK_U01 is able to analyze basic problems in differential equations with respect to application of suitable approximate methods

PEK_U02 is able to construct mathematical models used in concrete applications of mathematics, based on differential equations and their discrete forms.

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relating to social competences:

PEK_K01 can, without assistance, search for necessary information in the literature

PEK_K02 understands necessity of systematic and individual work on the material of the course.

PROGRAMME CONTENT

Form of classes - lecture		Number of hours
Lec 1	Recalling basic facts of theory of ordinary differential equations.	2
Lec 2	Explicit and implicit Euler method of approximate solving of ordinary differential equations and their systems.	2
Lec 3	Runge-Kutta type methods and other schemes of approximation of ordinary differential equations and their systems.	2
Lec 4	Multi-step methods, stability of numerical methods. Stiff problems.	2
Lec 5	Methods of approximation of boundary value problems for second order ordinary differential equations: shooting methods and difference methods.	2
Lec 6	Methods of approximation of boundary value problems for second order ordinary differential equations: Ritz-Galerkin method.	2
Lec 7	Difference methods for first order partial differential equations. CFL condition.	2
Lec 8	Recalling basic facts of theory of second order partial differential equations.	2
Lec 9	Difference approximation of elliptic boundary value problems on the plane.	2
Lec 10	Variational formulation of boundary value problems for elliptic type equations.	2
Lec 11	Ritz-Galerkin and finite element methods for elliptic problems.	2
Lec 12	Difference methods for parabolic problems. Explicit and implicit schemes for heat conduction equation.	2
Lec 13	Stability of approximate method. Crank-Nicholson scheme for equations of parabolic type.	2
Lec 14	Difference methods for the vibrating string problem and other	4

	hyperbolic problems.	
	Total hours	30

Form of classes - laboratory		Number of hours
Lab 1	Computer construction of solution of ordinary differential equations.	4
Lab 2	Practical verifying of efficacy of automatic exactness control.	2
Lab 3	Visualization and comparison of usefulness of various methods.	4
Lab 4	Algorithms for numerical methods of solution of one-dimensional boundary value problems for elliptic equations.	4
Lab 5	Discretisation of hyperbolic first order problems. Conditions of stability and convergence of approximate methods.	4
Lab 6	Discretization of two-dimensional boundary value problem for elliptic equations.	4
Lab 7	Difference schemes of approximation of one-dimensional parabolic equation.	4
Lab 8	Difference method of discretization of the vibrating string equation.	4
	Total hours	

TEACHING TOOLS USED
N1. Lecture – traditional method. N2. Problem and computing laboratory – traditional and using computers method. N3. Consultations. N4. Student’s personal work – preparation for the laboratory.

EVALUATION OF SUBJECT EDUCATIONAL EFFECTS ACHIEVEMENT

Evaluation (F – forming (during semester), P – concluding (at semester end))	Educational effect number	Way of evaluating educational effect achievement
F1	PEK_W01 PEK_W02 PEK_K01	Presentation of given problems.
F2	PEK_U01 PEK_U02 PEK_K01	Oral presentations, tests.
$P=0.5 \cdot F1 + 0.5 \cdot F2$		

PRIMARY AND SECONDARY LITERATURE

PRIMARY LITERATURE:

- [1] Richard L. Burden, J. Douglas Faires, Numerical Analysis.
- [2] R. M. Mattheij, S. W. Rienstra, J.H.M. ten Thijsse Boonkamp, Partial differential equations. Modeling, analysis and computations.
- [3] Stig Larsson, Vidar Thomee, Partial differential equations with numerical methods.

SECONDARY LITERATURE

- [1] L. Lapidus, G. F. Pinder, Numerical solution of partial differential equations in science and engineering, John Wiley & Sons, 1998
- [2] R. J. Le Veque, Numerical Methods for conservation laws, Birkhauser, Basel 1990
- [3] J. W. Thomas, Numerical partial differential equations: conservation laws and elliptic equations, Springer, New York 1999

SUBJECT SUPERVISOR (NAME AND SURNAME, E-MAIL ADDRESS)

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**MATRIX OF CORRELATION BETWEEN EDUCATIONAL EFFECTS FOR
SUBJECT
NUMERICAL METHODS IN DIFFERENTIAL EQUATIONS MAT001570
AND EDUCATIONAL EFFECTS FOR MAIN FIELD OF STUDY
MATHEMATICS
AND SPECIALIZATION MATHEMATICS FOR INDUSTRY AND
COMMERCE**

Subject educational effect	Correlation between subject educational effect and educational effects defined for main field of study and specialization (if applicable)**	Subject objectives***	Programme content***	Teaching tool number***
PEK_W01 (knowledge)	K2MST_W03 K2MST_mic_W01	C1-C3	Lec1- Lec14	1,3
PEK_W02	K2MST_W10 K2MST_mic_W02 K2MST_mic_W03	C1-C3	Lec1- Lec14	1,3
PEK_U01 (skills)	K2MST_U15, K2MST_U24 K2MST_U25 K2MST_U28 K2MST_U29 K2MST_mic_U01	C1-C3	La1-La8	2,3,4
PEK_U02	K2MST_U16 K2MST_mic_U02 K2MST_mic_U03	C1-C3	La1-La8	2,3,4
PEK_K01 (competences)	K2MST_K06 K2MST_mic_K01	C1-C3	Lec1- Lec14, La1-La8	1,2,3,4
PEK_K02	K2MST_K01 K2MST_mic_K02	C1-C3	Lec1- Lec14, La1-La8	1,2,3,4

** - enter symbols for main-field-of-study/specialization educational effects

*** - from table above