

**FACULTY OF PURE AND APPLIED MATHEMATICS****SUBJECT CARD****Name in Polish: Funkcje Specjalne****Name in English: Special Functions****Main field of study (if applicable): MATHEMATICS****Specialization (if applicable):****Level and form of studies: 2nd level, full-time / ~~part-time~~\*****Kind of subject: obligatory / ~~optional~~ / ~~university-wide~~\*****Subject code MAT001379****Group of courses YES / ~~NO~~\***

	Lecture	Classes	Laboratory	Project	Seminar
Number of hours of organized classes in University (ZZU)	30	30			
Number of hours of total student workload (CNPS)	150				
Form of crediting	Examination				
For group of courses mark (X) final course	X				
Number of ECTS points	5				
including number of ECTS points for practical (P) classes	3				
including number of ECTS points for direct teacher-student contact (BK) classes	3				

\*delete as applicable

**PREREQUISITES RELATING TO KNOWLEDGE, SKILLS AND OTHER COMPETENCES**

1. Knowledge of analysis of functions of several variables
2. Knowledge of complex analysis

**SUBJECT OBJECTIVES**

- C1 Recognition of definitions and basic properties of special functions  
 C2 Recognition of asymptotics of special functions

**SUBJECT EDUCATIONAL EFFECTS**

relating to knowledge:

PEK\_W01 Knows basic special functions

PEK\_W02 Knows basic asymptotics of special functions

relating to skills:

PEK\_U01 Knows how to use special functions

relating to social competences:

PEK\_K01

PEK\_K02

<b>PROGRAMME CONTENT</b>		
<b>Form of classes - lecture</b>		<b>Number of hours</b>
Lec 1	Gamma, Beta and Zeta functions	4
Lec 2	Differential equations of second order	2
Lec 3	Orthogonal polynomials: Hermite, Laguerre, Jacobi polynomials (including Legendre polynomials).	2
Lec 4	Discrete orthogonal polynomials	2
Lec 5	Cylindrical functions: Bessel functions of first, second and third order, their asymptotics, zeroes and recurrence properties.	4
Lec 6	Hypergeometric functions: definition, recurrence properties, associated differential equation, integral representation.	4
Lec 7	Confluent hypergeometric functions: definition, recurrence properties, associated differential equation, integral representation.	4
Lec 8	Asymptotics	4
Lec 9	Elliptic functions	4
	Total hours	<b>30</b>

<b>Form of classes - class</b>		<b>Number of hours</b>
Cl 1	Solving problems illustrating subjects from lectures	
	Total hours	30

<b>TEACHING TOOLS USED</b>
N1. Lecture – classic method.
N2. Exercises, computational and others – classic method.

#### **EVALUATION OF SUBJECT EDUCATIONAL EFFECTS ACHIEVEMENT**

<b>Evaluation</b> (F-forming (during semester), P – concluding (at semester end))	<b>Educational effect number</b>	<b>Way of evaluating educational effect achievement</b>
F1	PEK_W1, PEK_W2, PEK_K1	Examination
F2	PEK_U1, PEK_K1	Oral answers, partial exams
C=0.5*F1+0.5*F2		

<b>PRIMARY AND SECONDARY LITERATURE</b>
<b><u>PRIMARY LITERATURE:</u></b> [1] N. N. <b>Lebedev</b> , Special functions, 1968. [2] B. C. Carlson, Special functions of applied mathematics, Academic Press, 1977.
<b><u>SECONDARY LITERATURE:</u></b> [3] I. M. Ryzhik, I. S. Gradshteyn, Tables of integrals, series and products , Alan Jeffrey and Daniel Zwillinger (eds.) 2007. [4] R. Beals, R. Wong, Special functions, Cambridge University Press, 2011. [5] G. N. Watson, A treatise on the theory of Bessel functions, Cambridge Univ. Press, 1922
<b><u>SUBJECT SUPERVISOR (NAME AND SURNAME, E-MAIL ADDRESS)</u></b>  prof. dr hab. Janusz Mierczyński ( <a href="mailto:janusz.mierczynski@pwr.edu.pl">janusz.mierczynski@pwr.edu.pl</a> ) prof. dr hab. Krzysztof Stempak ( <a href="mailto:krzysztof.stempak@pwr.edu.pl">krzysztof.stempak@pwr.edu.pl</a> )

MATRIX OF CORRELATION BETWEEN EDUCATIONAL EFFECTS FOR  
 SUBJECT  
**Special functions**  
 AND EDUCATIONAL EFFECTS FOR MAIN FIELD OF STUDY  
 MATHEMATICS

Subject educational effect	Correlation between subject educational effect and educational effects defined for main field of study and specialization (if applicable)**	Subject objectives***	Programme content***	Teaching tool number***
PEK_W01 (knowledge)	K2MAT_W03	C1	Lec 1-9	1
PEK_W02	K2MAT_W09	C1	Lec 1-9	1
PEK_U01 (skills)	K2MAT_U15	C1	Cl 1	2
PEK_K01 (competences)	K2MAT_K06	C1	Lec 1-9, Cl 1	1,2

\*\* - enter symbols for main-field-of-study/specialization educational effects

\*\*\* - from table above