FACULTY OF COMPUTER SCIENCE AND MANAGEMENT

## SUBJECT CARD

MATHEMATICAL ANALYSIS I
analiza Matematyczna I
Computer Science
Specialization (if applicable)
Level and form of studies
Kind of subject
Subject code
Group of courses
I level, full time
obligatory
MAT001689
YES

|  | Lecture | Exercise class | Laboratory | Project | Seminar |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of hours of organized <br> University classes (ZZU) | 30 | 30 |  |  |  |
| Number of hours of total student <br> workload (CNPS) |  |  |  |  |  |
| Form of crediting | exam | crediting with <br> grade |  |  |  |
| For a group of courses mark the <br> final course (X) | X |  |  |  |  |
| Number of ECTS points | 6 |  |  |  |  |
| including number of ECTS <br> points for practical (P) classes |  |  |  |  |  |
| including number of ECTS <br> points for direct teacher-student <br> contact (BK) classes |  |  |  |  |  |

## PREREQUISITES RELATING TO KNOWLEDGE, SKILLS AND OTHER COMPETENCES

Knowledge of mathematics equivalent to high school certificate at the advanced level is recommended.

## SUBJECT OBJECTIVES

C1 Provide training in basic elementary functions and their properties.
C2 Provide training in basic differential calculus of one-variable functions.
C3 Introduction to the concept of definite integral, its basic properties and methods of calculation.
C4 Presentation of practical applications of differential and integral calculus of one-variable functions.

| SUBJECT EDUCATIONAL EFFECTS |
| :--- |
| Relating to knowledge a student: |
| PEK_W1 knows graphs and properties of basic elementary functions, |
| PEK_W2 knows basic notions and theorems of differential calculus for one-variable functions, |
| PEK_W3 knows the concept of definite integral, its properties and basic applications. |
| Relating to skills a student: |
| PEK_U1 can solve typical equations and inequalities with elementary functions, |

PEK_U2 can examine a function and draw its graph, PEK_U3 can evaluate typical indefinite integrals and calculate definite integrals, PEK_U4 can apply differential and integral calculus to solve practical problems.

| PROGRAMME CONTENT |  |  |
| :---: | :---: | :---: |
| Form of classes - lecture |  | Hours |
| Lec1 | Definition of a function. Basic examples: linear, quadratic and polynomial functions. Rational functions. Composition of functions. Transformations of graphs of functions. | 3 |
| Lec2 | Injective functions. The inverse function and its graph. Power and exponential functions and their inverses. Properties of logarithms. | 2 |
| Lec3 | Trigonometric functions. Unit (trigonometric) circle. Inverse trigonometric functions. | 2 |
| Lec4 | Sequences of real numbers. Finite and infinite limit of a sequence. Basic theorems on limits of sequences. Indeterminate expressions. The number $e$. | 3 |
| Lec5 | The limit of a function at a point and the limit at infinity. Examples of the limits of certain indeterminate expressions. Asymptotes. | 2 |
| Lec6 | Continuity of a function at a point and on an interval. Basic properties of continuous functions. Approximate solutions of equations. | 2 |
| Lec7 | The derivative of a function. Geometrical and physical interpretations of the derivative. Tangent line. Differential of a function. Derivatives of basic elementary functions. Differentiation rules. | 2 |
| Lec8 | Lagrange's theorem. Intervals of monotonicity of a function. De l'Hospital's rule. | 2 |
| Lec9 | Local and global extrema. Examples of optimization problems. | 2 |
| Lec 10 | Definition and basic properties of indefinite integral. Basic rules. The substitution rule and integration by parts. | 2 |
| Lec 11 | Definition and basic properties of definite integral. Fundamental theorem of calculus (Newton-Leibniz theorem). | 2 |
| Lec12 | Applications of integral calculus (average value of a function, area of a flat region, volumes of solids of revolution, arc length etc.) | 2 |
| Lec 13 | Integration of rational and trigonometric functions. | 2 |
| Lec14 | Examples of applications of mathematical analysis methods for one-variable functions (e.g. Taylor's theorem, convexity and inflection points of a function, or other applications typical for the field of study). | 2 |
|  | Total hours | 30 |
|  | Form of classes - classes | Hours |
| Cl1 | Elements of mathematical logic (logical connectives, quantifiers). Determination of the function domain. Even and odd functions. | 2 |
| C12 | Composition of functions. Transformations of graphs of functions. Polynomial and rational equations and inequalities. | 2 |
| Cl3 | The inverse function. Typical equations and inequalities with exponential and logarithmic functions. | 2 |
| C14 | Trigonometric and inverse trigonometric functions. Unit (trigonometric) circle. Typical trigonometric equations and inequalities. | 2 |
| C15 | Monotonicity and boundedness of sequences. Computing proper and improper limits of sequences. | 2 |
| C16 | Limits of functions. Asymptotes. | 2 |
| C17 | Continuity of a function. Approximate solutions of equations. | 2 |
| C18 | Derivative of a function. Rules of differentiation. Tangent line. Differentials and their applications. | 2 |
| C19 | De l'Hospital's rule. Intervals of monotonicity of a function. | 2 |


| Cl10 | Determining local and global extrema of a function. | 2 |
| :---: | :--- | :---: |
| Cl11 | Evaluation of indefinite integrals of elementary functions. Integration by parts and by <br> substitution. | 2 |
| Cl12 | Calculating definite integrals. Area of a flat region as an application of definite integral. | 2 |
| Cl13 | Applications of definite integral. | 2 |
| Cl14 | Integration of rational and trigonometric functions. | 2 |
| Cl15 | Test. | 2 |
|  |  | Total hours |

## TEACHING TOOLS USED

N1 Lectures - traditional or using multimedia tools.
N2 Classes - traditional method (problems sessions and discussion).
N3 Student's self-study with the assistance of mathematical packages.
N4 Tutorial.

## EVALUATION OF SUBJECT EDUCATIONAL EFFECTS ACHIEVEMENT

| Evaluation (F - forming; <br> P - concluding) | Educational effect number | Way of evaluating educational effect <br> achievement |
| :--- | :--- | :--- |
| F-Cl | PEK_U1-PEK_U4, <br> PEK_K1 | tests, oral presentations, quizzes |
| F-Lec | PEK_W1-PEK_W3 | exam |
| P - rules set by the lecturer |  |  |

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## PRIMARY AND SECONDARY LITERATURE

 <br> PRIMARY LITERATURE: <br> [1] G. Decewicz, W. Żakowski, Matematyka, Cz.1, WNT, Warszawa 2007. <br> [2] M. Gewert, Z. Skoczylas, Analiza matematyczna 1. Definicje, twierdzenia, wzory, Oficyna Wydawnicza GiS, Wrocław, 2015. <br> [3] M. Gewert, Z. Skoczylas, Analiza matematyczna 1. Przykłady i zadania, Oficyna Wydawnicza GiS, Wrocław, 2015. <br> [4] W. Krysicki, L. Włodarski, Analiza matematyczna w zadaniach, Cz. I, PWN, Warszawa, 2006. <br> \section*{SECONDARY LITERATURE:} <br> [1] F. Leja, Rachunek różniczkowy i całkowy, PWN, 2012. <br> [2] R. Leitner, Zarys matematyki wyższej dla studiów technicznych, cz.1-2, WNT, Warszawa, 2006. <br> [3] M. Zakrzewski, Markowe wykłady z matematyki. Analiza, Oficyna Wydawnicza GiS, Wrocław, 2013.}

## SUBJECT SUPERVISORS

Wydziałowa Komisja Programowa ds. kursów ogólnouczelnianych dr Jolanta Sulkowska (Jolanta.Sulkowska@ pwr.edu.pl)

## CORRELATION MATRIX BETWEEN EDUCATIONAL EFFECTS FOR SUBJECT <br> MATHEMATICAL ANALYSIS I MAT1689 <br> AND EDUCATIONAL EFFECTS FOR MAIN FIELD OF STUDY Computer Science

| Subject <br> educationa <br> l effect | Correlation between <br> subject educational <br> effect and educational <br> effects defined for <br> main field of study and <br> specialization (if <br> applicable) | Subject <br> objectives | Programme content | Teaching <br> tool <br> number |
| :---: | :---: | :---: | :--- | :---: |
| PEK_W1 | K1INF_W01 | C1 | Lec1-Lec6 | N1-N4 |
| PEK_W2 | K1INF_W01 | C2 | Lec7-Lec9, Lec14 | N1-N4 |
| PEK_W3 | K1INF_W01 | C3 | Lec10-Lec13 | N1-N4 |
| PEK_U1 | K1INF_W01 | C1 | Lec1-Lec3, Cl1-Cl4 | N1-N4 |
| PEK_U2 | K1INF_W01 | C1 | Lec5-Lec9, Cl5-Cl10 | N1-N4 |
| PEK_U3 | K1INF_W01 | C3 | Lec10, Lec11, Lec13, Cl11, Cl12, Cl14 | N1-N4 |
| PEK_U4 | K1INF_W01 | C2, C4 | Lec7, Lec12, Lec14, C18-Cl10, Cl12, Cl13 | N1-N4 |

